

Sec 1.5 Volume of Right Pyramids and Right Cones

Volume

↳ the amount of space an object occupies, measured in cubic units.

Recall from Grade 8

$$\begin{aligned}\text{Volume of any prism} &= \textit{Area of the Base} \times \textit{Height} \\ &= B \times H\end{aligned}$$



this changes
depending on the
shape of the prism

Rectangular Prism



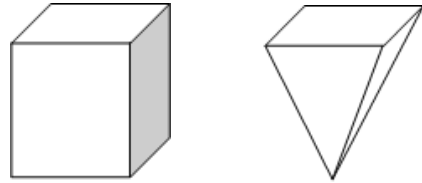
Cylinder




Investigation 1.5: Volumes of Right Pyramids and Right Cones

Part A:

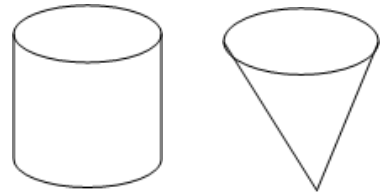
The right prism and a right pyramid given has equal bases and equal heights.




1. What is the formula for the volume for a right rectangular prism?
2. Fill the pyramid with water, without overflowing! Pour the water from the pyramid into the prism. How many full pyramids fill the prism? Take a guess first!
3. What conclusion can you make about the relationship between the volumes of a right prism and a right pyramid with equal bases and equal heights?

4. What is the formula for the **volume** of a right rectangular pyramid?

Part B:

The right cylinder and a right cone given has equal bases and equal heights.



1. What is the formula for the volume for a right cylinder?
2. Fill the cone with water, without overflowing! Pour the water from the cone into the cylinder. How many full cones fill the cylinder? Take a guess first!
3. What conclusion can you make about the relationship between the volumes of a right cylinder and a right cone with equal bases and equal heights?

4. What is the formula for the **volume** of a right **cone**?

Summary after Investigation

Volume of a right rectangular pyramid



Volume of a right cone



Note:

This relationship between right prisms and right pyramids is true for any shaped base, as long as they have the same base and height.

Example 1

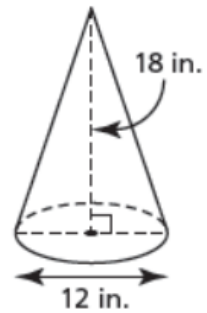
Determine the volume of a right rectangular pyramid with base dimensions 5.4 cm by 3.2 cm and height 8.1 cm. Round the answer to the nearest tenth of a cubic centimeter.

Example 2

A cylinder has volume of 312 cm^3 . What is the volume of a cone that has the same base and height as the cylinder?

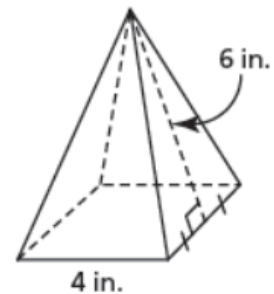
Example 3

Determine the volume of this cone to the nearest cubic inch.



Example 4

Calculate the volume of this right square pyramid to the nearest cubic inch.



Example 5

A cone has a height of 4 yd. and a volume of 205 yd^3 . Determine the radius of the base of the cone to the nearest yard.

Work Book Questions

p.42 #4a, 5a, 6a, 7a, 8b, 9b, 10ab,
11ab, 12, 18abcd

Extra Practice Questions

p.42 #4b, 5b, 6b, 7b, 8a, 9a,
13b, 14ac, 19b